

# How to model legal reasoning using dynamic logic programming: a preliminary report

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## **Abstract.**

Dynamic logic programming allows the representation and the inference of evolving knowledge.

Legal knowledge reasoning needs the capability to model laws that change over time and to model laws produced by distinct entities with different priorities at different time points.

In this paper we propose the use of dynamic logic programming to model these legal dynamic situations. Some examples are discussed and the implementation of a legal oracle server is described.

## **1 Introduction**

It is well known that knowledge representation needs to take into account the dynamic nature of knowledge. As new information is acquired, new pieces of knowledge need to be dynamically added to or removed from the knowledge bases. Moreover, information may be produced from different sources having different degrees of reliability and, as a consequence, having different priorities.

In [2] dynamic logic programming was proposed as a possible solution to the problem of knowledge base updates and in [3] a new language, *LUPS – Language of UPdateS*, was described and applied to the representation of actions.

On the other hand, legal knowledge reasoning needs the capability to model laws that change over time and to model laws produced by distinct entities with different priorities at different time points. These problems have been studied by several researchers, being Prakken and Sartor's work one of the most relevant [8, 10]. In their work they have proposed an argument-based extended logic programming framework with defeasible priorities. In another work, Sartor [7] and Provetti [11] have proposed the use of Event Calculus [5] as the base formalism to model time. A complete survey about the existent approaches to the use of logic to model legal reasoning was presented in [9].

In this paper we propose the use of dynamic logic programming to model some legal dynamic situations. Specifically, we will deal with the representation of evolving rules and with the problem of having several sources of laws with possible contradictions.

In order to fully explore these situations, a legal server was implemented in Prolog and it is able to receive logic programming descriptions of laws and events and to answer queries about what is valid in specific states. Some simple examples are described and discussed.

At this stage, it is important to point out that we do not claim that dynamic logic programming is able to deal with every legal reasoning situation. This paper is just a preliminary step in this direction.

In section 2 the logic programming framework used to model the legal server is presented. Then, in section 3, the legal server implementation is briefly described and in section 4, examples of hypothetical server interactions are presented. Finally, in section 5 some conclusions and future work are pointed out.

## 2 Dynamic Logic Programming

Before describing the legal server it is necessary to present the formalism used to implement it. As referred in the previous section, the basic formalism is the dynamic logic programming paradigm and the related language used to represent actions: LUPS<sup>1</sup>.

### 2.1 Dynamic Knowledge Representation

One of the main requirements of the formalism used to represent legal knowledge is to be able to handle evolving knowledge. In fact, legal knowledge may be represented by specific knowledge states but, after each event, such as a law change, knowledge evolves to another state. The formalism should be able to handle these situations, allowing the inference of what properties are valid in each knowledge state.

Dynamic logic programming (DLP) was proposed [2] as a possible solution to this evolution requirement. In fact, DLP defines how a knowledge base can be updated by another knowledge base, obtaining a new knowledge base.

Specifically, given an original knowledge base  $KB$ , and an updating knowledge base  $KB'$ , it is possible to obtain a new updated knowledge base  $KB^* = KB \oplus KB'$  that constitutes the update of the knowledge base  $KB$  by the knowledge base  $KB'$ . In order to make the meaning of the updated knowledge base  $KB \oplus KB'$  declaratively clear and easily verifiable, in [2] there is a complete semantic characterisation of the updated knowledge base  $KB \oplus KB'$ . In this work, knowledge bases are defined by sets of generalized logic programs and the updated knowledge base is obtained by a linear-time transformation of the knowledge bases  $KB$  and  $KB'$  into normal logic programs. The basic idea is to add new logic programming rules for modeling inheritance, update, and default situations (the transformation is fully described in the referred paper). As a result, not only the update transformation can be accomplished very efficiently, but also query answering in  $KB \oplus KB'$  is reduced to query answering about normal logic programs using the stable model semantics.

### 2.2 LUPS – Language of UPdateS

In DLP, a knowledge base evolves from one knowledge state <sup>2</sup> to another as a result of a knowledge update. Given the current knowledge state  $KS$ , its successor knowledge state  $KS' = KS \oplus KB$  is obtained as a result of the occurrence of a non-empty set of simultaneous updates, represented by the updating knowledge base  $KB$ .

However, dynamic knowledge updates, do not provide any language allowing the specification of knowledge state changes. Accordingly, in [3] it was described a fully declarative, high-level language for knowledge updates called LUPS “Language of UPdateS”) that

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<sup>1</sup>This section is based on a previous work describing DLP and LUPS [4]

<sup>2</sup>In this context, a knowledge state can be viewed as a snapshot of the knowledge base at a specific point (state).

describes transitions between consecutive knowledge states  $KS_n$ . It consists of update commands, which specify what updates should be applied to any given knowledge state  $KS_n$  in order to obtain the next knowledge state  $KS_{n+1}$ . In this way, update commands allow us to implicitly determine the updating knowledge base  $KB_{n+1}$ . The language LUPS can therefore be viewed as a language for dynamic knowledge representation.

The simplest update command consists of adding a rule to the current knowledge state and has the form:  $assert(L \leftarrow L_1, \dots, L_k)$ . For example, when a law stating that abortion is illegal is adopted, the knowledge state might be updated via the command:  $assert(illegal \leftarrow abortion)$ .

In general, the addition of a rule to a knowledge state may depend upon some preconditions being true in the current state. To allow for that, the assert command in LUPS has a more general form:

$$assert(L \leftarrow L_1, \dots, L_k) \text{ when } (L_{k+1}, \dots, L_m) \quad (1)$$

The meaning of this assert command is that if the preconditions  $L_{k+1}, \dots, L_m$  are true in the current knowledge state, then the rule  $L \leftarrow L_1, \dots, L_k$  should hold true in the successor knowledge state. Normally, the so added rules are *inertial*, i.e., they remain in force from then on by inertia, until possibly defeated by some future update or until retracted.

However, in some cases the persistence of rules by inertia should not be assumed. Take, for instance, the simple action *request help*. This is likely to be a one-time event that should not persist by inertia after the successor state. Accordingly, the assert command allows for the keyword *event*, indicating that the added rule is *non-inertial*.

$$assert \text{ event } (L \leftarrow L_1, \dots, L_k) \text{ when } (L_{k+1}, \dots, L_m) \quad (2)$$

Update commands themselves (rather than the rules they assert) may either be one-time, non-persistent update commands or they may remain in force until cancelled. In order to specify such *persistent update commands* (which are called *update laws*) there is the syntax:

$$always [\text{event}] (L \leftarrow L_1, \dots, L_k) \text{ when } (L_{k+1}, \dots, L_m) \quad (3)$$

Note the word *event* is optional and it defines if the update command should persist or if it is only a one-time command.

To cancel persistent update commands, we use:

$$cancel(L \leftarrow L_1, \dots, L_k) \text{ when } (L_{k+1}, \dots, L_m) \quad (4)$$

To deal with rule deletion, there is the *retraction* update command:

$$retract(L \leftarrow L_1, \dots, L_k) \text{ when } (L_{k+1}, \dots, L_m) \quad (5)$$

meaning that, subject to precondition  $L_{k+1}, \dots, L_m$ , the rule  $L \leftarrow L_1, \dots, L_k$  is retracted.

The main difference between *cancel* and *retract* is that the first is used to cancel persistent *always* commands and the other is used to cancel *assert* commands.

Knowledge can be queried at any knowledge state  $KS_q$  with:

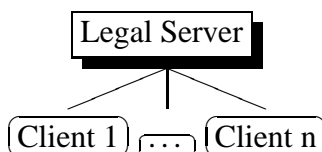
$$\mathbf{holds} B_1, \dots, B_k, \text{ not } C_1, \dots, \text{ not } C_m \mathbf{ at state } q? \quad (6)$$

and is true if and only if the conjunction of its literals holds at the state  $KS_q$ . In this equation  $q$  stands for an identifier of the knowledge state (it can be defined as an integer being 0 the identifier for the initial knowledge state); *not* stands for the default negation and the predicate *holds* verifies if the literals belong to the stable model of the knowledge base  $KS_q$ .

The language LUPS has a *declarative and procedural semantics* [2] so that the update commands not only have a definite declarative meaning but also can be readily implemented. The procedural semantics for LUPS is obtained by the translation of the LUPS program into a *normal logic program*, written in a *meta-language*. The translation of LUPS into XSB-Prolog is available at <http://centria.di.fct.unl.pt/~jja/updates/lups.p>

### 3 Legal Server

The legal server is a XSB-Prolog process able to deal with connections via a user defined TCP/IP port. The overall architecture is presented in figure 1.



**Figure 1:** Architecture

There are two possible commands that clients may send to the legal server:

- Update
- Query

The clients send sequences of update rules and/or queries about properties and they receive the answers to their queries.

These commands will be described in detail in the next two sub-sections:

#### 3.1 Update command

The update rules have the following syntax:

$$\text{update}(KB, Agent, LUPSSList) \quad (7)$$

where  $KB$  means knowledge base and allowing the definition and the update of distinct knowledge bases;  $Agent$  defines the name of the agent performing the action; and  $LUPSSList$  is a Prolog list of LUPS commands.

As an example, we may have:

$$\text{update}(\text{law}, \text{crimeLaw}, [(\text{always}(\text{illegal} \leftarrow \text{abortion}))]) \quad (8)$$

It is also possible to use predicate *update* with only two arguments,  $KB$  and  $LUPSSList$ , meaning we want to update or to query the KB as a top priority independent agent. This special top agent has also the possibility to define priorities among the different agents:

$$\text{higherPriority}(Agent1, Agent2). \quad (9)$$

The priority relations will have important consequences in the processing of the agents updates.

After receiving an update predicate, the legal server will create corresponding LUPS updates, evolving the  $KB$  received as a parameter to a new state. The translation between the client requests (rule 7) and the LUPS updates follows these rules:

1. For every request received from agent *Agent1*
  - (a) For every LUPS command in LUPSList having a rule with head *H* create a corresponding command, substituting *H* by  $H_{Agent1}$
  - (b) For each distinct predicate *H* (head of some LUPS command) introduced by the request, create the new rule:

$$always (H \leftarrow H_{Agent1}, not - H_{A1}, \dots, not - H_{An}) \quad (10)$$

where  $A1, \dots, An$  are agents with higher priority than *Agent1* and *not* and  $-$  stand for the default and explicit negation, respectively.

The general idea of the first part of the translation is to index every conclusion (head of the rules) to the corresponding agent. The second part of the translation relates the agents beliefs with its more priority agents: an agent belief is only accepted if it is not contradictory with a belief of another more priority agent.

As a simple example, rule 8 would produce the following LUPS rules:

$$always (illegal_{crimeLaw} \leftarrow abortion) \quad (11)$$

$$always (illegal \leftarrow illegal_{crimeLaw}) \quad (12)$$

If, for instance, Constitutional Law is an agent of a higher priority, then we would have the following rule (instead of rule 12):

$$always (illegal \leftarrow illegal_{crimeLaw}, not - illegal_{constitutionalLaw}) \quad (13)$$

### 3.2 Query command

The query commands have the following syntax:

$$query(KB, Agent, \mathbf{holds} B_1, \dots, B_k, not C_1, \dots, not C_m \mathbf{at state} q?) \quad (14)$$

where *KB* means knowledge base and allowing the query of distinct knowledge bases; *Agent* defines the name of the agent performing the action.

As in the previous section, it is possible to omit the second parameter and to query the *KB* from the special top agent. As an example, we may have:

$$query(law, \mathbf{holds} illegal \mathbf{at state} now^3?) \quad (15)$$

## 4 Examples

In the next two sub-sections two kind of examples will be presented:

- Evolution of laws
- Laws produced by distinct agents/entities

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<sup>3</sup>*now* stands for the integer identifier of the actual knowledge state. Users are allowed to use identifier *now* and, even, to define arithmetic operations with it: *now - 1* standing for the previous state.

## 4.1 Evolution of laws

Suppose there is a law stating that in order to have a specific degree it is necessary to be enrolled in that degree and to verify certain conditions:

$$\text{update}(\text{law1}, [\text{assert}(\text{degree}(X) \leftarrow \text{enrolled}(X), \text{cond1}(X))]). \quad (16)$$

Now, suppose John enrolls himself in that degree:

$$\text{update}(\text{law1}, [\text{assert}(\text{enrolled}(\text{john}))]). \quad (17)$$

But, after that, there is an update in the law and the needed conditions change:

$$\begin{aligned} \text{update}(\text{law1}, [\text{retract}(\text{degree}(X) \leftarrow \text{enrolled}(X), \text{cond1}(X)), \\ \text{assert}(\text{degree}(X) \leftarrow \text{enrolled}(X), \text{cond2}(X))]). \end{aligned} \quad (18)$$

After this change John verifies *cond1* and Mary enrolls herself in the degree:

$$\text{update}(\text{law1}, [\text{assert}(\text{cond1}(\text{john})), \text{assert}(\text{enrolled}(\text{mary}))]). \quad (19)$$

Finally, Mary satisfies *cond2*:

$$\text{update}(\text{law1}, [\text{assert}(\text{cond2}(\text{mary}))]). \quad (20)$$

If we query the *KB* about who has a degree and in which states:

$$\text{query}(\text{law1}, \mathbf{holds} \text{ degree}(X) \mathbf{ at state } S?). \quad (21)$$

We will obtain the behavior:

$$X = \text{mary}, S = 5.$$

Only Mary has a degree and only at state 5 (we are assuming initial state to be equal to 0).

Note that, if we change update 17 to:

$$\text{update}(\text{law1}, [\text{assert}(\text{enrolled}(\text{john})), \text{assert}(\text{cond1}(\text{john}))]). \quad (22)$$

We would get:

$$\begin{aligned} X = \text{john}, S = 2; \\ X = \text{mary}, S = 5. \end{aligned}$$

This answer reflects the fact that rule defining how to obtain a degree has changed. However, law updates are usually not retroactive: if John had a degree at state 2, then he shouldn't have lost his degree afterwards!

This requisite leads to a new schema for the representation of law changes<sup>4</sup>:

$$\text{update}(\text{law2}, [\text{assert}(\text{degree}(X) \leftarrow \text{en}(X), \text{cond1}(X))]). \quad (23)$$

$$\text{update}(\text{law2}, [\text{assert}(\text{en}(\text{john}))]). \quad (24)$$

$$\begin{aligned} \text{update}(\text{law2}, [\text{retract}(\text{degree}(X) \leftarrow \text{en}(X), \text{cond1}(X)) \text{ when } (\text{not } \text{en}(X)), \\ \text{assert}(\text{degree}(X) \leftarrow \text{en}(X), \text{cond2}(X)) \text{ when } (\text{not } \text{en}(X))]). \end{aligned} \quad (25)$$

$$\text{update}(\text{law2}, [\text{assert}(\text{cond1}(\text{john})), \text{assert}(\text{en}(\text{mary}))]). \quad (26)$$

$$\text{update}(\text{law2}, [\text{assert}(\text{cond2}(\text{mary}))]). \quad (27)$$

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<sup>4</sup>Due to formatting problems we will use *en* instead of the predicate *enrolled*

Rule 25 captures the notion that the law changes only to those that are not yet enrolled in the degree.

As intended, we'll have:

$$X = john, S = 4;$$

$$X = john, S = 5;$$

$$X = mary, S = 5.$$

#### 4.2 Laws from distinct entities

In this example we will try to show that LUPS and DLP are also able to model prioritised rules without many changes.

Suppose there are three sources of knowledge defining what is needed to obtain a master's degree (conditions necessary and sufficient):

- S1: To write a thesis;
- S2: To obtain a certain amount of course credits;
- S3: To write a thesis and to obtain a certain amount of course credits (100 in this example).

We'll have the following corresponding commands:

$$\begin{aligned} \text{update}(\text{law3}, s1, [\text{assert}(\text{master}(X) \leftarrow \text{thesis}(X)), \\ \text{assert}(\neg \text{master}(X) \leftarrow \neg \text{thesis}(X))]). \end{aligned} \quad (28)$$

$$\begin{aligned} \text{update}(\text{law3}, s2, [\text{assert}(\text{master}(X) \leftarrow \text{credits}(X, N), N > 100), \\ \text{assert}(\neg \text{master}(X) \leftarrow \text{credits}(X, N), N \leq 100)]). \end{aligned} \quad (29)$$

$$\begin{aligned} \text{update}(\text{law3}, s3, [\text{assert}(\text{master}(X) \leftarrow \text{credits}(X, N), N > 100, \\ \text{thesis}(X)), \\ \text{assert}(\neg \text{master}(X) \leftarrow (\text{credits}(X, N), N \leq 100; \\ \neg \text{thesis}(X)))]). \end{aligned} \quad (30)$$

Suppose agents are related by the following relation  $s1 < s2 < s3$ :

$$\text{higherPriority}(s3, s2). \quad (31)$$

$$\text{higherPriority}(s2, s1). \quad (32)$$

With these constraints, the following update facts:

$$\text{update}(\text{law3}, [\text{assert}(\text{thesis}(john))]). \quad (33)$$

$$\text{update}(\text{law3}, [\text{assert}(\text{credits}(mary, 120))]). \quad (34)$$

$$\text{update}(\text{law3}, [\text{assert}(\text{credits}(john, 110))]). \quad (35)$$

And the following queries:

$$\text{query}(\text{law3}, \text{holds } \text{master}_{s1}(X) \text{ at state } S?). \quad (36)$$

$$\text{query}(\text{law3}, \text{holds } \text{master}_{s2}(X) \text{ at state } S?). \quad (37)$$

$$\text{query}(\text{law3}, \text{holds } \text{master}_{s3}(X) \text{ at state } S?). \quad (38)$$

$$\text{query}(\text{law3}, \text{holds } \text{master}(X) \text{ at state } S?). \quad (39)$$

We'll have:

$$\begin{aligned} & \text{master}_{s_1}(\text{john}), S = 4; \\ & \text{master}_{s_1}(\text{john}), S = 5; \\ & \text{master}_{s_1}(\text{john}), S = 6; \\ & \text{master}_{s_2}(\text{mary}), S = 5; \\ & \text{master}_{s_2}(\text{mary}), S = 6; \\ & \text{master}_{s_3}(\text{john}), S = 6; \\ & \text{master}(\text{john}), S = 6; \end{aligned}$$

These results, as intended, state that according with  $S_1$  John has a master's degree after terminating his thesis (state 4); accordingly with  $S_2$  this is accomplished only at state 6 for John (and 5 for Mary); and accordingly with  $S_3$  only John has a master's degree and only at state 6. As  $S_3$  is the most priority agent, its "opinion" is the accepted by the legal server.

## 5 Conclusions and Future Work

The use of dynamic logic programming and its associated language, LUPS, to model some characteristics of legal reasoning was proposed. Specifically, the problem of laws that change over time and the problem of laws produced by different sources with different reliabilities/priorities was dealt with.

Dynamic logic programming revealed to be a powerful methodology to handle these kind of requisites and the obtained solutions were quite satisfactory and easy to model. A legal server able to receive law updates and requests was also implemented. These server is able to handle requests from different agents and about different knowledge bases.

As future work, we intend to use an extension of DLP, MDLP – Multidimensional Dynamic Logic Programming, from J. Leite et al. [6] to allow a more generic approach and the integration of several dimensions, such as time and priorities, and to compare it with other existent approaches, such as Prakken and Sartor's work.

Another possible direction is to use the new language, EVOLP, proposed by Alferes et. al [1], to simplify LUPS.

We also intend to change the communication protocol to a standard agent communication protocol, such as FIPA ACL [12]. In this way, our legal agent may be able to interact with a larger community of computational agents.

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